# PRODUCTION OF SCALAR BOSON AND NEUTRINO PAIR IN LONGITUDINALLY POLARIZED ELECTRON-POSITRON COLLIDING BEAMS

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Within the framework of the Minimal Supersymmetric Standard Model, the processes of the production of a scalar boson in longitudinally polarized electron-positron collisions are investigated:  $e^-e^+ \rightarrow H_V \bar{\nu}$ ,  $e^-e^+ \rightarrow h_V \bar{\nu}$ , where  $V \bar{V}$  is the neutrino-antineutrino pair. It is shown that each process is described by two spiral amplitudes  $F_{LR}$  and  $F_{RL}$  that describe the processes

 $e_L^-e_R^+ \to H(h)v\overline{v}$  and  $e_R^-e_L^+ \to H(h)v\overline{v}$  accordingly. Two mechanisms for the creation of a scalar boson have been studied in detail: the radiation of a scalar boson by a vector  $Z^0$ -boson and the production of a scalar boson as a result of the fusion of  $W^+W^-$ -

bosons. An analytic expression of the effective cross sections is obtained, which describe the angular and energy distributions of the scalar boson.

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## 1. INTRODUCTION

The Standard Model (SM), based on the local gauge symmetry group  $SU_C(3) \times SU_L(2) \times U_4(1)$ , has achieved great success in describing the strong, electromagnetic, and weak interactions between elementary particles [1-3]. With the recent discovery of the scalar Higgs boson at the Large Hadron Collider (LHC) by the ATLAS and CMS laboratories [4-5] (see also the reviews [6-8]) the CM of fundamental interactions has got a logical conclusion. We note that the SM contains one scalar doublet that provides a mass to  $W^{\pm}$ ,  $Z^0$ -bosons, quarks, and leptons simultaneously. In this case, there is only one CP-even Higgs boson  $H_{CM}$ . The SM extension is the Minimal Supersymmetric Standard Model (MSSM), where, unlike SM, two doublets of scalar complex fields with hypercharges -1 and 1 are introduced [8-11]:

$$H_1 = \begin{pmatrix} H_1^0 \\ H_1^- \end{pmatrix}, \qquad H_2 = \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix}.$$

Scalar fields are written as:

$$H_{1} = \frac{1}{\sqrt{2}} \begin{pmatrix} \vec{v}_{1} + H_{1}^{0} + iP_{1}^{0} \\ H_{1}^{-} \end{pmatrix}, \quad H_{2} = \frac{1}{\sqrt{2}} \begin{pmatrix} H_{2}^{+} \\ \vec{v}_{2} + H_{2}^{0} + iP_{2}^{0} \end{pmatrix},$$

where  $H_1^0$ ,  $P_1^0$ ,  $H_2^0$  and  $P_2^0$  are real scalar fields,  $\upsilon_1$  and  $\upsilon_2$  are the vacuum values of the fields  $\langle H_1 \rangle = \frac{1}{\sqrt{2}} \upsilon_1$ 

and  $\langle H_2 \rangle = \frac{1}{\sqrt{2}} \upsilon_2$ .

CP-even H and h-bosons are obtained by mixing the fields  $H_1^0$   $\mu$   $H_2^0$  ( $\alpha$  the mixing angle):

$$\begin{pmatrix} H \\ h \end{pmatrix} = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} H_1^0 \\ H_2^0 \end{pmatrix}.$$

Similarly, we get Goldstone's  $G^0$ ,  $G^{\pm}$ , CP odd A and charged  $H^{\pm}$ -bosons ( $\beta$  mixing angle):

$$\begin{pmatrix} G^{0} \\ A \end{pmatrix} = \begin{pmatrix} \cos\beta & \sin\beta \\ -\sin\beta & \cos\beta \end{pmatrix} \begin{pmatrix} P_{1}^{0} \\ P_{2}^{0} \end{pmatrix}, \quad \begin{pmatrix} G^{\pm} \\ H^{\pm} \end{pmatrix} = \begin{pmatrix} \cos\beta & \sin\beta \\ -\sin\beta & \cos\beta \end{pmatrix} \begin{pmatrix} H_{1}^{\pm} \\ H_{2}^{\pm} \end{pmatrix}$$

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Thus, there are five Higgs bosons in the MSSM: two CP-even bosons  $h, H, \ldots$  one CP-odd A-boson and two charged  $H^{\pm}$  bosons. Here the Higgs boson sector is characterized by six parameters:  $M_H, M_h, M_A, M_{H^{\pm}}, \alpha$  and  $\beta$ . Of these, only two parameters are free:  $M_A$  and  $tg\beta$ . The masses of the CP-even h- and H-bosons are expressed in terms of the masses  $M_A$  and  $M_Z$ :

$$M_{h(H)}^{2} = \frac{1}{2} \bigg[ M_{A}^{2} + M_{Z}^{2} \mp \sqrt{\left(M_{A}^{2} + M_{Z}^{2}\right)^{2} - 4M_{A}^{2}M_{Z}^{2}\cos^{2}2\beta} \bigg],$$

and the value  $\cos^2(\beta - \alpha)$  is given by the relation:

$$\cos^{2}(\beta - \alpha) = \frac{M_{h}^{2}(M_{Z}^{2} - M_{h}^{2})}{M_{A}^{2}(M_{H}^{2} - M_{h}^{2})}$$

The parameter  $tg\beta$  is equal to the ratio of the vacuum values of the fields  $H_2^0$  and  $H_1^0$  ( $tg\beta = v_2/v_1$ ) varies within the limits  $1 \le tg\beta \le m_t/m_b$ , where  $m_t$  and  $m_b$  is the mass of t- and b-quarks.

In the present paper we have studied the processes of the production of a scalar H (or h) boson and a neutrino pair on longitudinally polarized electron-positron colliding beams:

$$e^- + e^+ \to H + v + \overline{v} \,, \tag{1}$$

$$e^- + e^+ \to h + v + \overline{v} \tag{2}$$

where  $v\bar{v}$  is a pair of muon, tau-lepton or electron neutrinos ( $v\bar{v} \Rightarrow v_{\mu}\bar{v}_{\mu}, v_{\tau}\bar{v}_{\tau}, v_{e}\bar{v}_{e}$ ).

## 2. THE MECHANISM OF EMISSION OF A SCALAR BOSON

The Feynman diagrams of the reaction (1) are shown in Fig. 1. In brackets are written 4-particle momentum, electron and positron helicity. We note that diagram a) corresponds to the emission of a scalar boson by a vector  $Z^0$ -boson.



*Fig. 1.* Feynman diagrams of the reaction  $e^-e^+ \rightarrow Hv_e \overline{v}_e$ .

Diagram a) corresponds to the following matrix element (here, the conservation of electron and neutrino currents is taken into account, and also  $p^2 = (p_1 + p_2)^2 > M_Z^2$ ):

$$M_{a}(e^{-}e^{+} \rightarrow Hv\bar{v}) = i \left(\frac{e}{2\sin\theta_{W}\cdot\cos\theta_{W}}\right)^{3} \cdot M_{Z}\cos(\beta-\alpha) D_{Z}(s) D_{Z}(xs) \times \\ \times \vec{v}(p_{2},\lambda_{2})\gamma_{\mu} \left[g_{L}(1+\gamma_{5}) + g_{R}(1-\gamma_{5})\right] u(p_{1},\lambda_{1}) \cdot \bar{u}(q_{1})\gamma_{\mu}(1+\gamma_{5})v(q_{2}),$$
(3)

where  $\theta_{W}$  is the Weinberg angle,

$$D_Z(s) = (s - M_Z^2)^{-1}, \quad D_Z(xs) = (xs - M_Z^2 + iM_Z\Gamma_Z)^{-1},$$

 $M_Z$  and  $\Gamma_Z$  the mass and total width of the  $Z^0$ -boson,  $s = p^2$  the square of the total energy of the  $e^-e^+$ -pair in the center-of-mass system,  $g_L$  and  $g_R$  the left and right coupling constants of the electron with the  $Z^0$ -boson

$$g_L = -\frac{1}{2} + x_W, \quad g_R = x_W,$$
 (4)

 $x_W = \sin^2 \theta_W$  – the Weinberg parameter, x – the invariant mass of the neutrino pair in units s:

$$x = \frac{q^2}{s} = \frac{(q_1 + q_2)^2}{s} = 1 - \frac{2E_H}{\sqrt{s}} + \frac{M_H^2}{s},$$
(5)

 $E_H$  and  $M_H$  is the energy and mass of the scalar boson H.

At high energies in weak interactions the helicity of the particles is conserved. Preservation of helicity requires that the colliding electron and positron have opposite helicities:  $e_L^- e_R^+$  or  $e_R^- e_L^+$ . Here  $e_L^-$  – the left-polarized electron  $(\lambda_1 = -1)$ , and  $e_R^+$  – the right-handed positron  $(\lambda_2 = +1)$ . Thus, the process (1) has two spiral amplitudes:  $F_{LR}$  and  $F_{RL}$  (the first and second indices correspond to the helicities of the electron and the positron, respectively). These spiral amplitudes describe the processes  $e_L^- + e_R^+ \rightarrow H + v + \bar{v}$  and  $e_R^- + e_L^+ \rightarrow H + v + \bar{v}$  are given by the expressions:  $F_{LR} = D_Z(s)D_Z(xs)g_L$ ,  $F_{RL} = D_Z(s)D_Z(xs)g_R$ .

First we consider the matrix element of the process  $e_L^- + e_R^+ \rightarrow H + v + \overline{v}$ :

$$M_{a}(e_{L}^{-}e_{R}^{+} \rightarrow Hv\bar{v}) = i \left(\frac{e}{2\sin\theta_{w}\cdot\cos\theta_{w}}\right)^{3} \cdot M_{Z}\cos(\beta-\alpha) \cdot F_{LR} \times [\vec{v}(p_{2},\lambda_{2}=1)\gamma_{\mu}(1+\gamma_{5})u(p_{1},\lambda=-1_{1})] \cdot [\vec{u}(q_{1})\gamma_{\mu}(1+\gamma_{5})v(q_{2})]$$
(7)

and draw it square:

$$\left|M_{a}(\bar{e_{L}e_{R}^{+}} \to Hv\bar{v})\right|^{2} = \left(\frac{e^{2}}{4x_{w}(1-x_{w})}\right)^{3}M_{Z}^{2}\cos^{2}(\beta-\alpha)\left|F_{LR}\right|^{2}T_{\mu\nu}^{(1)}T_{\mu\nu}^{(2)}.$$
(8)

Here

$$T_{\mu\nu}^{(1)} = 8[p_{1\mu}p_{2\nu} + p_{2\mu}p_{1\nu} - (p_1 \cdot p_2)g_{\mu\nu} - i\varepsilon_{\mu\nu\rho\sigma}p_{1\rho}p_{2\sigma}],$$
  

$$T_{\mu\nu}^{(2)} = 8[q_{1\mu}q_{2\nu} + q_{2\mu}q_{1\nu} - (q_1 \cdot q_2)g_{\mu\nu} + i\varepsilon_{\mu\nu\alpha\beta}q_{1\alpha}q_{2\beta}]$$
(9)

- tensors of electron-positron and neutrino pairs. The product of these tensors gives a simple expression:

$$T^{(1)}_{\mu\nu} \cdot T^{(2)}_{\mu\nu} = 2^8 (p_1 \cdot q_2) (p_2 \cdot q_1) = 2^8 p_{1\alpha} p_{2\beta} q_{2\alpha} q_{1\beta}.$$
(10)

We integrate over momentum of neutrino and antineutrino pair by the invariant methods [12-15]:

$$I_{\alpha\beta} = \int q_{2\alpha} q_{1\beta} \cdot \frac{d\vec{q}_1}{\omega_1} \cdot \frac{d\vec{q}_2}{\omega_2} \,\delta(q_1 + q_2 - q) = A \cdot q^2 \,g_{\alpha\beta} + Bq_\alpha q_\beta, \tag{11}$$

where A and B are scalar functions, and a q = p - k is the total 4-momentum of the neutrino pair. To find the scalar functions A and B, we first multiply the integral  $I_{\alpha\beta}$  by the tensor  $g_{\alpha\beta}$ , and then by  $q_{\alpha}q_{\beta}$ . The result is a system of equations

$$g_{\alpha\beta}I_{\alpha\beta} = \frac{1}{2}q^{2}I = 4Aq^{2} + Bq^{2},$$

$$q_{\alpha}q_{\beta}I_{\alpha\beta} = \frac{1}{4}q^{4}I = 4Aq^{4} + Bq^{4},$$
(12)

where the integral

$$I = \int \frac{d\vec{q}_1}{\omega_1} \cdot \frac{d\vec{q}_2}{\omega_2} \,\delta(q_1 + q_2 - q)$$

it is easily calculated in the center of mass system of neutrinos and antineutrinos, and is equal to  $2\pi$ . From the system of equations (12) we obtain:

$$A = \frac{\pi}{6}, \quad B = \frac{\pi}{3}.$$

Thus, for the integral  $I_{\alpha\beta}$  we have the expression:

$$I_{\alpha\beta} = \frac{\pi}{6} (q^2 g_{\alpha\beta} + 2q_{\alpha} q_{\beta}).$$
<sup>(13)</sup>

As a result of integrating the neutrinos and antineutrinos momentum for the differential cross section of the process  $e_L^- + e_R^+ \Longrightarrow H + v + \overline{v}$  in the center-of-mass system we obtain:

$$\frac{d\sigma_a(e_L^-e_R^+ \Longrightarrow Hv\bar{v})}{dE_H d(\cos\theta)} = \frac{1}{12} \left(\frac{\alpha_{K\Im\mathcal{A}}}{x_w(1-x_w)}\right)^3 M_Z^2 s k_H \cos^2(\beta-\alpha) \left|F_{LR}\right|^2 \left(2x + \frac{1}{s}k_H^2 \sin^2\theta\right). \tag{14}$$

Here  $k_H = \sqrt{E_H^2 - M_H^2}$  is the momentum modulus of the scalar boson *H*,  $\theta$  is the angle of emission of the *H* boson with respect to the momentum of the electron.

Similarly, we obtain the expression for the cross section of the reaction  $e_R^- + e_L^+ \Longrightarrow H + v + \overline{v}$ :

$$\frac{d\sigma_a(e_R^-e_L^+ \to Hv\bar{\nu})}{dE_H d(\cos\theta)} = \frac{1}{12} \left(\frac{\alpha_{KED}}{x_W(1-x_W)}\right)^3 M_Z^2 s k_H \cos^2(\beta-\alpha) |F_{RL}|^2 \left(2x + \frac{1}{s} k_H^2 \sin^2\theta\right).$$
(15)

In the case of annihilation of a longitudinally polarized  $e^-e^+$ -pair, the contribution of diagram a) to the differential cross section of the reaction  $e^- + e^+ \rightarrow H + v + \overline{v}$  is given by:

$$\frac{d\sigma_a(\lambda_1, \lambda_2)}{dE_H d(\cos\theta)} = \frac{1}{96} \left(\frac{\alpha_{KED}}{x_W (1 - x_W)}\right)^3 M_Z^2 s k_H \cos^2(\beta - \alpha) \times \left[|F_{RL}|^2 (1 - \lambda_1)(1 + \lambda_2) + |F_{RL}|^2 (1 + \lambda_1)(1 - \lambda_2)\right] \left(2x + \frac{1}{s}k_H^2 \sin^2\theta\right).$$

## 3. MECHANISM OF FUSION OF $W^+W^-$ -BOSONS

Now consider the diagram b) corresponding to the fusion mechanism of charged vector bosons. The matrix ele-

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ment corresponding to this diagram is written as follows:

$$M_{b}(e^{-}e^{+} \rightarrow Hv_{e}\bar{v}_{e}) = i\frac{e^{3}M_{W}}{8\sin^{3}\theta_{W}} \cdot \cos(\beta - \alpha)D_{1} \cdot D_{2} \times$$

$$[\overline{u}(q_1)\gamma_{\mu}(1+\gamma_5)u(p_1,\lambda_1)]\cdot[\overline{\upsilon}(p_2,\lambda_2)\gamma_{\mu}(1+\gamma_5)\upsilon(q_2)]$$
(18)

Here

$$D_{1} = (k_{1}^{2} - M_{W}^{2})^{-1}, \quad D_{2} = (k_{2}^{2} - M_{W}^{2})^{-1},$$
  

$$k_{1} = p_{1} - q_{1}, \quad k_{2} = p_{2} - q_{2},$$
(19)

 $M_W$  – mass of a charged W-boson.

The square of the matrix element (18) is equal to:

$$\left| M_{b}(e^{-}e^{+} \to Hv_{e}\bar{v}_{e}) \right|^{2} = \left( \frac{e^{3}M_{W}}{\sin^{3}\theta_{W}} \right)^{2} \cos^{2}(\beta - \alpha)(D_{1} \cdot D_{2})^{2}(1 - \lambda_{1})(1 + \lambda_{2})(p_{2} \cdot q_{1})(p_{1} \cdot q_{2}).$$
(20)

The integration over momentum of neutrinos and antineutrinos is carried out in the center of mass system of this pair  $\vec{q}_1 + \vec{q}_2 = 0$  (see Fig. 2). In this system we have [14, 15]:

$$\int |M_{b}|^{2} \cdot \frac{d\vec{q}_{1}}{\omega_{1}} \cdot \frac{d\vec{q}_{2}}{\omega_{2}} \delta(p_{1} + p_{2} - k - q_{1} - q_{2}) = \int |M_{b}|^{2} d\omega_{1} d(\cos\theta_{1}) d\varphi_{1} \delta(E_{1} + E_{2} - E_{H} - 2\omega_{1}) =$$

$$= \frac{1}{2} \int_{-1}^{1} d(\cos\theta_{1}) \int_{0}^{2\pi} |M_{b}|^{2} d\varphi_{1}$$
(21)

The square of the amplitude  $|M_b|^2$  can be represented in the form (here it is taken into account that  $q_2 = p_1 + p_2 - k - q_1$ ):

$$\left|M_{b}\right|^{2} = \frac{1}{2} \left(\frac{e^{3}M_{W}}{\sin^{3}\theta_{W}}\right) \cdot \cos^{2}(\beta - \alpha) \frac{(1 - \lambda_{1})(1 - \lambda_{2}) \cdot [s - 2(k \cdot p_{1}) - 2(p_{1} \cdot q_{1})](p_{2} \cdot q_{1})}{[2(p_{1} \cdot q_{1}) + M_{W}^{2}]^{2} [s + M_{W}^{2} - 2(k \cdot p_{2}) - 2(p_{2} \cdot q_{1})]^{2}}.$$
 (22)

We note that in the expression  $|M_b|^2$  the dependence on the azimuth angle  $\varphi_1$  appears only in the scalar product  $(p_2 \cdot q_1)$ . In the coordinate system under consideration, we have:

$$(p_1 \cdot q_1) = \frac{1}{4} [s - 2(k \cdot p_1)](1 - \cos \theta_1),$$
  
$$(p_2 \cdot q_1) = \frac{1}{4} [s - 2(k \cdot p_2)](1 - \cos \theta_1 \cos \chi - \sin \theta_1 \sin \chi \cos \varphi_1).$$

but  $\cos \chi$  is expressed by invariant variables:

$$\cos \chi = 1 - \frac{2s[s + M_H^2 - 2(k \cdot p_1) - 2(k \cdot p_2)]}{[s - 2(k \cdot p_1)[s - 2(k \cdot p_2)]}.$$
(23)

The integration over the azimuth angle  $\varphi_1$  is easily carried out:

$$\int_{0}^{2\pi} |M_{b}|^{2} d\varphi_{1} \sim \frac{1}{s_{1}s_{2}(h_{1} - \cos\theta_{1})^{2}} \bigg[ 2(h_{2} + \cos\theta_{1}\cos\chi) \cdot (1 + \cos\theta_{1}) \times (1 + \cos\theta_{1}) \bigg] \bigg]$$

$$\times \left(1 + \frac{M_W^2}{s_2}\right) \cdot \frac{1}{R\sqrt{R}} - (1 + \cos\theta_1) \cdot \frac{1}{R} \right], \tag{24}$$

the notations are given by

$$s_{1} = s - 2(k \cdot p_{1}), \qquad s_{2} = s - 2(k \cdot p_{2}),$$

$$h_{1} = 1 + \frac{2M_{W}^{2}}{s_{1}}, \qquad h_{2} = 1 + \frac{2M_{W}^{2}}{s_{2}},$$

$$R = \cos^{2}\theta_{1} + 2h_{2}\cos\theta_{1}\cos\chi + h_{2}^{2} - \sin^{2}\chi.$$
(25)

The integrals over the polar angle  $\theta_1$  are easily calculated.



*Fig. 2.* The center of mass  $v\overline{v}$  -pair system.

After integrating over the angles  $\theta_1$  and  $\varphi_1$ , for the differential cross section the following expression was obtained:

$$\frac{d\sigma_b(e^-e^+ \Rightarrow Hv_e\bar{v}_e)}{dE_H d(\cos\theta)} = \frac{M_Z^2}{4} \left(\frac{\alpha_{KED}}{x_W(1-x_W)}\right)^3 \cdot \frac{k_H}{s} \cos^2(\beta-\alpha)(1-\lambda_1)(1+\lambda_2) \cdot F_W.$$
(26)

Here

$$F_{W} = \frac{(1-x_{W})^{4}}{s_{1}s_{2}r} \left\{ (1+h_{1})(1+h_{2}) \left[ \frac{2}{h_{1}^{2}-1} + \frac{2}{h_{2}^{2}-1} - \frac{6\sin^{2}\chi}{r} + \left( \frac{3t_{1}t_{2}}{r} - \cos\chi \right) \frac{L}{\sqrt{r}} \right] - \left[ \frac{2t_{1}}{h_{2}-1} + \frac{2t_{2}}{h_{1}-1} + (t_{1}+t_{2}+\sin^{2}\chi) \frac{L}{\sqrt{r}} \right] \right\}$$
(27)  
$$s_{1} = \sqrt{s} \left( \sqrt{s} - E_{H} + k_{H} \cos\theta \right), \quad s_{2} = \sqrt{s} \left( \sqrt{s} - E_{H} - k_{H} \cos\theta \right),$$
$$\cos\chi = 1 - \frac{2xs}{xs + k_{H}^{2} \sin^{2}\theta}, \quad \sin^{2}\chi = 1 - \cos^{2}\chi,$$
$$t_{1} = h_{1} + h_{2} \cos\chi, \quad t_{2} = h_{2} + h_{1} \cos\chi, \quad r = h_{1}^{2} + h_{2}^{2} + 2h_{1}h_{2} \cos\chi - \sin^{2}\chi,$$
$$L = \ln\frac{h_{1}h_{2} + \cos\chi + \sqrt{r}}{h_{1}h_{2} + \cos\chi - \sqrt{r}}$$

In the process of production of a neutrino pair  $v_e \overline{v}_e$  between diagrams a) and b), there is an interference. The interference contribution to the cross section is given by:

$$\frac{d\sigma(e^-e^+ \Rightarrow Hv_e \bar{v}_e)}{dE_H d(\cos\theta)} = \frac{M_Z^2}{4} \left(\frac{\alpha_{K\Im\mathcal{A}}}{x_W(1-x_W)}\right)^3 \cdot \frac{k_H}{s} \cos^2(\beta - \alpha)(1-\lambda_1)(1+\lambda_2)g_L F_I, \tag{28}$$

where

$$F_{I} = \frac{1}{2} (1 - x_{W})^{2} \frac{xs - M_{Z}^{2}}{(s - M_{Z}^{2})[(xs - M_{Z}^{2}) + M_{Z}^{2}\Gamma_{Z}^{2}]} \times \left[2 - (h_{1} + 1)\ln\frac{h_{1} + 1}{h_{1} - 1} - (h_{2} + 1)\ln\frac{h_{2} + 1}{h_{2} - 1} + (h_{1} + 1)(h_{2} + 1)\frac{L}{\sqrt{r}}\right].$$
(29)

## 4. DISCUSSION OF THE RESULTS

The differential cross section of the reaction  $e^- + e^+ \rightarrow H + v_e + \overline{v}_e$  measured in the experiments consists of three parts: the contribution of diagram a), the contribution of diagram b), and the interference contribution. At the energies of a  $e^-e^+$ -pair  $\sqrt{s} > M_Z$ , the differential cross section has the form:

$$\frac{d\sigma(e^-e^+ \Rightarrow H\nu_e \overline{\nu}_e)}{dxd(\cos\theta)} = \frac{M_Z^2}{8} \left(\frac{\alpha_{KED}}{x_w(1-x_w)}\right)^3 \frac{k_H}{\sqrt{s}} \cos^2(\beta-\alpha) \times \left\{3[g_L^2(1-\lambda_1)(1+\lambda_2) + g_R^2(1+\lambda_1)(1-\lambda_2)]F_s + (1-\lambda_1)(1+\lambda_2)(g_L F_I + F_W)\}\right\}.$$
(30)

Here the function  $F_s$  corresponds to the contribution of diagram a) (the scalar boson *H* is emitted by the vector boson  $Z^0$ ):

$$F_{s} = \frac{1}{12} \cdot \frac{s(2xs + k_{H}^{2}\sin^{2}\theta)}{(s - M_{Z}^{2})^{2}[(xs - M_{Z}^{2})^{2} + M_{Z}^{2}\Gamma_{Z}^{2}]}.$$
(31)

The factor 3 in the first term (30) is associated with the possibility of decay of the  $Z^0$ -boson into three types of neutrino pair  $(v_e \bar{v}_e, v_\mu \bar{v}_\mu, v_\tau \bar{v}_\tau)$ . In the annihilation of a left-handed polarized electron and a right-polarized positron, we have a cross section:

$$\frac{d\sigma(e_L^- e_R^+ \Rightarrow Hv_e \bar{v}_e)}{dxd(\cos\theta)} = \left(\frac{\alpha_{KED}}{x_W(1 - x_W)}\right)^3 \cdot \frac{M_Z^2}{2} \cdot \frac{k_H}{\sqrt{s}} \cos^2(\beta - \alpha) [3g_L^2 F_s + g_L F_I + F_W].$$
(32)

If the electron (positron) is polarized right (left), then the contribution of diagram b) vanishes and the differential cross section takes the form:

$$\frac{d\sigma(e_{R}^{-}e_{L}^{+} \rightarrow Hv_{e}\overline{v}_{e})}{dxd(\cos\theta)} = \left(\frac{\alpha_{KED}}{x_{W}(1-x_{W})}\right)^{3} \frac{M_{Z}^{2}}{2} \cdot \frac{k_{H}}{\sqrt{s}} \cos^{2}(\beta-\alpha) \cdot 3g_{L}^{2}F_{s}.$$
(33)

In the case of unpolarized colliding electron-positron beams, the differential cross section of the reaction  $e^- + e^+ \rightarrow H + v + \overline{v}$  is expressed by the formula:

$$\frac{d\sigma(e^-e^+ \to Hv_e \bar{v}_e)}{dxd(\cos\theta)} = \frac{M_Z^2}{8} \left(\frac{\alpha_{KED}}{x_W(1-x_W)}\right)^3 \cdot \frac{k_H}{\sqrt{s}} \cdot \cos^2(\beta-\alpha) \cdot [3(g_L^2 + g_R^2)F_s + g_L F_I + F_W]. \tag{34}$$

On the fig. 3 shown the angular dependence of the *h*-boson in the reaction, at an energy of  $\sqrt{s} = 1000$  GeV, a mass of  $M_h = 67.533$  GeV, energy  $E_h = 2M_h$  and the Weinberg parameter  $x_W = 0.232$ . As can be seen from the

figure, with increasing boson emission angle, the contribution of the diagram *a*) increases and reaches a maximum at an angle of  $\theta = 90^{\circ}$ , and a further increase in the angle leads to a decrease in the cross section. But the contribution of diagram *b*) decreases with increasing angle  $\theta$  and reaches a minimum at  $\theta = 90^{\circ}$ . The contribution to the cross section from the interference of diagrams a) and b) is negative. The dependence of the total cross section of the process  $e^- + e^+ \rightarrow h + v_e + \bar{v}_e$  on the angle  $\theta$  in the fig. 3 is shown by the dotted line



Fig. 3. Angular dependence of the effective cross section of the process  $e^- + e^+ \rightarrow h + v_e + \bar{v}_e$ .

Similar results were obtained for the reaction  $e^- + e^+ \rightarrow H + v_e + \overline{v}_e$ .

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